



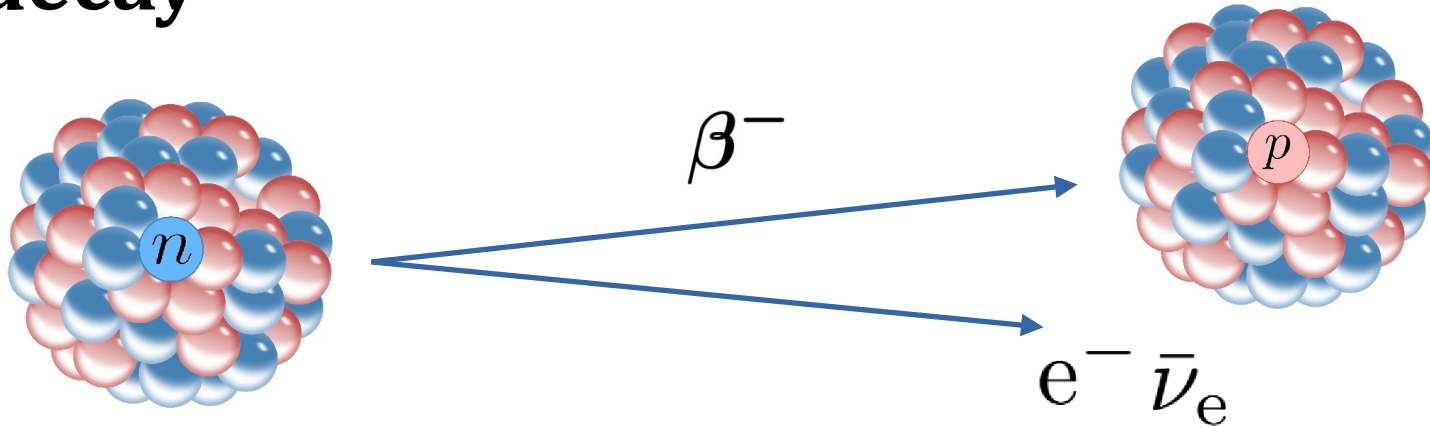
# **Double beta decay in the nuclear density functional theory**

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# Beta decay

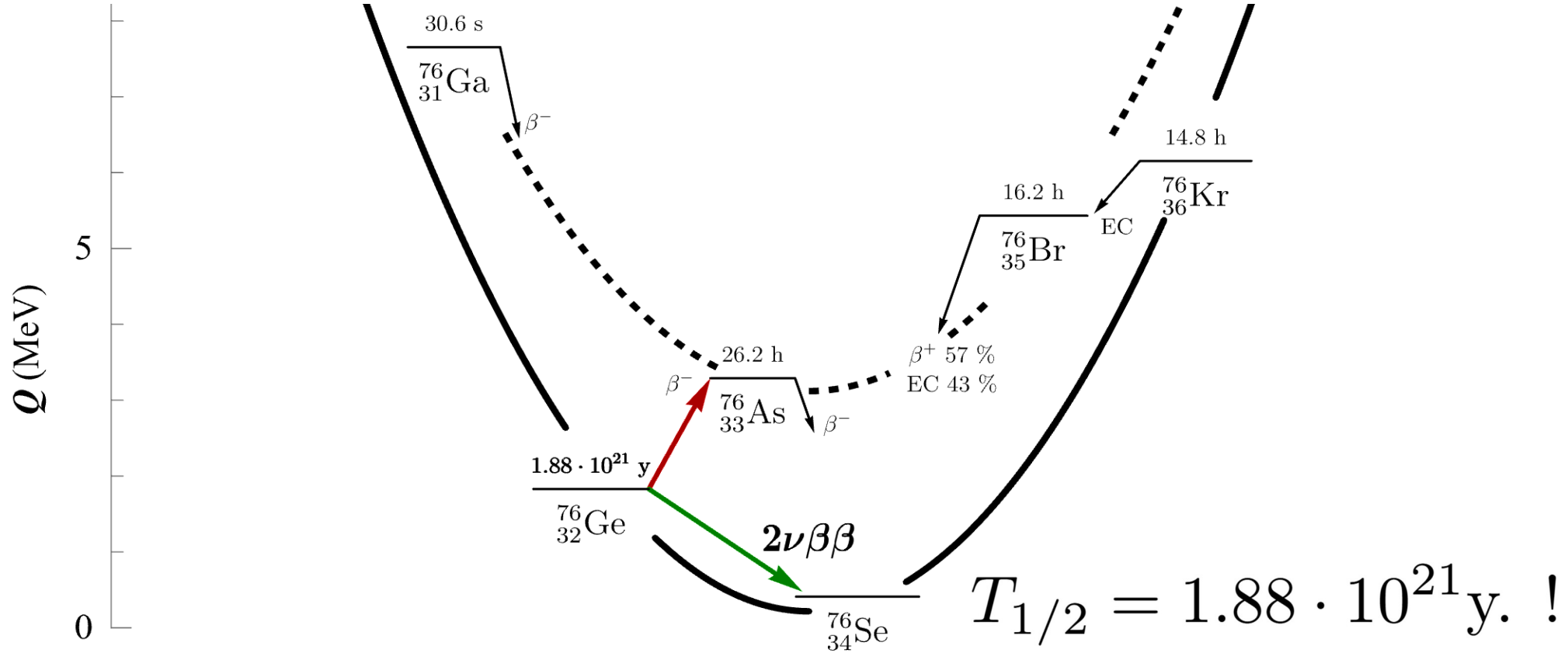


**Quantum-wise:** 
$$\hat{\mathcal{H}}_\beta = \frac{G_F}{\sqrt{2}} J^{\mu\dagger} j_\mu + \text{h.c.}$$

Annihilation-creation  
of a hadron (p,n)

Annihilation-creation  
of a lepton ( $e, \nu_e$ )

# Double beta decay



Energy parabolas of the even-even and odd-odd isobars of  $A=76$ .

Data from F. Kondev et al., Chinese Phys. C **45**, 030001 (2021).

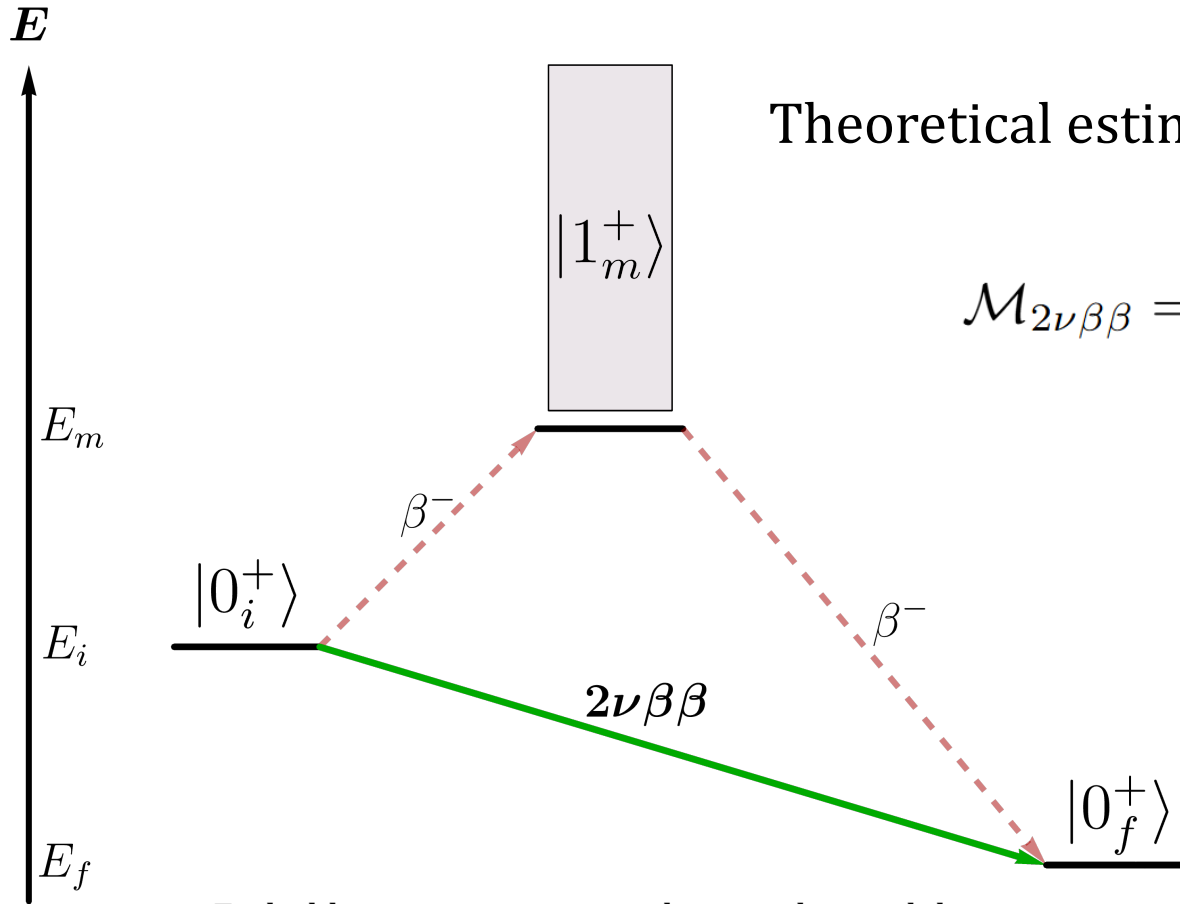
# Nuclear matrix element

$$T_{1/2}^{-1} = \underbrace{G_{2\nu\beta\beta}(Z, E)}_{\text{leptonic part}} \cdot \underbrace{|\mathcal{M}_{2\nu\beta\beta}|^2}_{\substack{\text{nuclear matrix element} \\ \text{(all nuclear QM)}}}$$

$$\sim G_F^4$$

***Extremely rare!***  
(only **11** nuclei)

# Fermi golden rule of the 2<sup>nd</sup> order



Theoretical estimation via **virtual** transitions:

$$\mathcal{M}_{2\nu\beta\beta} = \sum_m \frac{\langle 0_f^+ | \hat{H}_\beta | \mathbf{1}_m^+ \rangle \langle \mathbf{1}_m^+ | \hat{H}_\beta | 0_i^+ \rangle}{\Delta E_m + \frac{1}{2} Q_{\beta\beta} + \Delta M}$$

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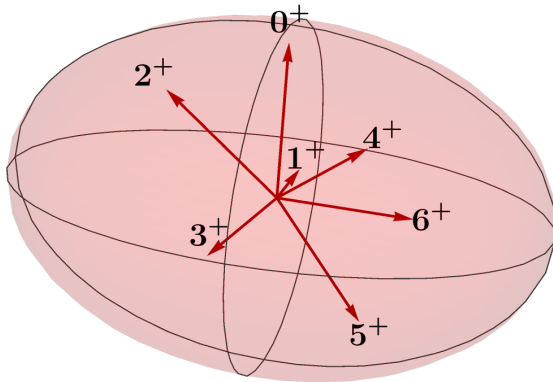
Key difficulty: constructing  
 $|0_i^+\rangle, |1_m^+\rangle, |0_f^+\rangle$

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Forbidden transitions contribute to the total decay rate.

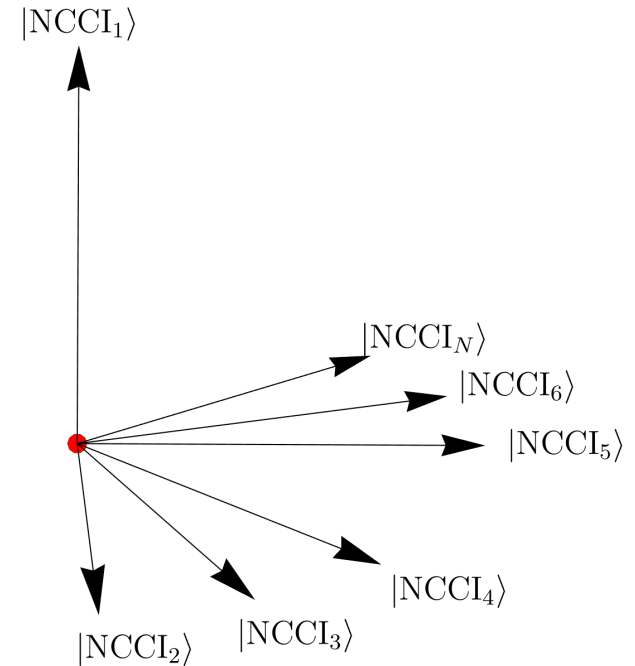
# NCCI based on Skyrme nuclear density functional

Kohn-Sham  $|\Psi_i\rangle$



no good quantum numbers  
 ~~$\gamma, \beta$~~  transitions

$I^\pi(T)$  – projection  
configuration mixing  
redialagonalization

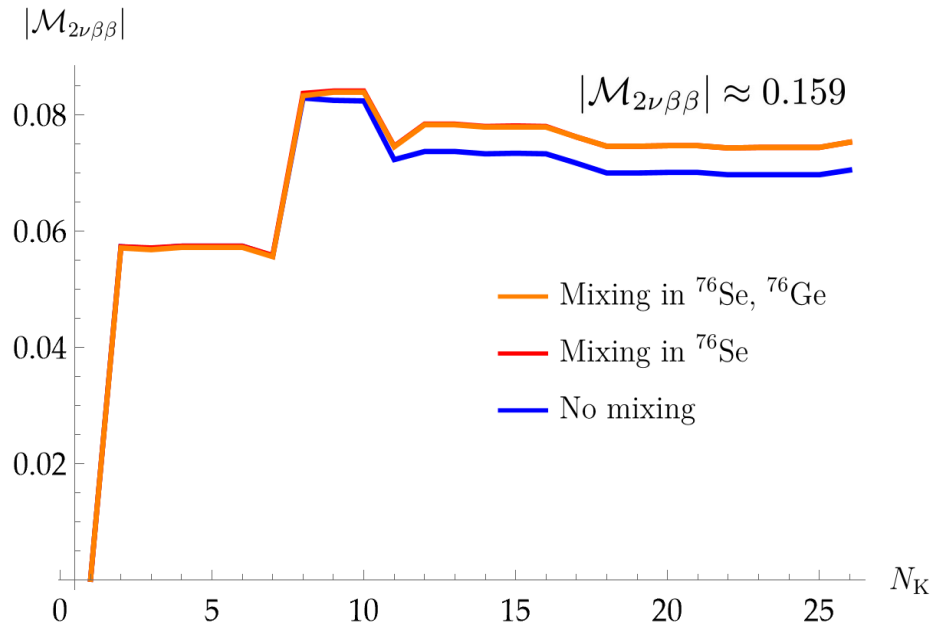


good quantum numbers  
 $\gamma, \beta$  transitions

# Status and future plans for the model

*Exemplary estimation for  
 $^{76}\text{Ge}$  nucleus*

*What next?*



Summing contributions from  $1^+_m$  up to saturation.

- $2\nu\beta\beta$  decay calculation of  $^{136}\text{Xe}$  (in progress) and other nuclei
- Implementation of neutrinoless matrix elements into NCCI framework
- Tests of the model on (hypothetical)  $0\nu\beta\beta$  decay.